

Dronacharya Group of Institutions, Greater Noida
Department of APS
Subject Name: Mathematics-II (KAS 203)
Lecture wise Question Bank

Unit No.: 4 Unit Name: Complex Variable-Differentiation

Lecture No.	Questions	Weightage of Question as per University Exam (In terms of Marks)	Reference
L1	Explain analytic function with the help of suitable examples.	2	
	Define necessary and sufficient condition for a mapping to be conformal.	2	
L2	Define Cauchy-Riemann equation	2	
	Prove by giving the example that a function is not analytic but Cauchy-Riemann equations are satisfied.	5	
L3	Prove that function with constant modulus is constant.	5	
	Find the value of c_1 and c_2 such that the function is analytic $= x^2 + c_1 y^2 - 2xy + i(c_2 x^2 - y^2 + 2xy)$	5	
L4	Show that $f(z) = \log z$ is analytic everywhere in the complex plane except at the origin.	5	
	Show that the function defined by $f(z) = \sqrt{ xy }$ is not regular at the origin, although Cauchy-Riemann equations are satisfied there.	5	
L5	Show that the function u is harmonic and find the corresponding analytic function $f(z) = x^3 - 3xy^2$	7	
	Find the image of $2x + y - 3 = 0$ under the transformation $w = z + 2i$.	5	
L6	Verify if $f(z)$ is analytic or not? $= \frac{xy^2(x+iy)}{x^2+y^4}, z \neq 0; f(0) = 0$	7	
	Determine the bilinear transformation which maps $z_1=0, z_2=1, z_3=\infty$ onto $w_1=i, w_2=-1, w_3=-i$ respectively.	5	
L7	Show that the following functions are harmonic and find their harmonic conjugate function $u = \frac{1}{2} \log(x^2 + y^2)$.	5	
	Determine the analytic function $f(z)$ in terms of z whose real part is $e^{-x}(x \sin y - y \cos y)$	7	